

Outline

- The N/S proximity system
 - The basics
 - NSN "critical voltage" (non-equilibrium / driven system)
- The F/S proximity system
 - How the basics change: oscillatory decay
 - Pairing types: singlet, triplet (1 x short-range, 2 x long-range)
 - Length scales
 - The FSF spin-valve
- Current experiments
 - Long-range triplet detection in a "forbidden" FSF structure
 - The physics beyond weak (exchange) limit

The (S/N) proximity effect



Superconducting correlations "leak" into N (near the interface)

- S becomes weaker (reduction of Δ)
- N obtains superconducting properties

This is "old" physics... are there still interesting things in standard N/S hybrids? Applying a voltage over an NSN junction gives an answer!!

Critical voltage



Inclusion of exchange field



Demler et al, PRB **55**, 1997

Why oscillations?

- Up and down potential energies are shifted differently.
- To balance total energy, kinetic energies are adjusted.
 - Result: interfering wave functions (due to different phase evolution)

What new physics to expect due to the exchange field?

- Oscillatory behavior with distance in (all) parameters depending on the gap
- Tuning device properties by adjusting the exchange field (like direction)
- Appearance of triplet pairing wave functions (in conventional S, only singlet)

$$\begin{array}{c} \text{Length scales of the oscillation}\\ \text{Linearized Usadel equation:}\\ (eigen)energy \\ \hline h \omega_n + i h_{ex} - \frac{1}{2} \hbar D \nabla^2 \end{pmatrix} F(\omega_n, x) = 0\\ \text{pair amplitude}\\ \text{field contribution kinetic term}\\ \text{General solution:} \quad F(\omega_n, x) = A e^{-x(k_1 + i k_2)} = A e^{-xk_1} (\cos(xk_2) + i \sin(xk_2))\\ \text{with} \quad k_{1,2} = \frac{1}{\xi_F} \sqrt{\sqrt{1 + \left[\frac{\hbar \omega_n}{h_{ex}}\right]^2} \pm \frac{\hbar \omega_n}{h_{ex}}} \quad \text{and} \quad \xi_F = \sqrt{\frac{\hbar D}{h_{ex}}}\\ \text{Some typical numbers}\\ \frac{k_1^{-1} \quad \text{characteristic decay length}}{2\pi k_2^{-1} \quad \text{period of the oscillation}}\\ \text{Field contribution} \quad \frac{5-20 \text{ meV} \quad 18-36 \text{ nm}}{135 \text{ meV} \quad 7 \text{ nm}}\\ \text{Field contribution} \quad \frac{5-20 \text{ meV} \quad 18-36 \text{ nm}}{135 \text{ meV} \quad 7 \text{ nm}}\\ \text{Field contribution} \quad \frac{5-20 \text{ meV} \quad 18-36 \text{ nm}}{155 \text{ meV} \quad 7 \text{ nm}}\\ \text{Field contribution} \quad \frac{5-20 \text{ meV} \quad 18-36 \text{ nm}}{155 \text{ meV} \quad 7 \text{ nm}}\\ \text{Field contribution} \quad \frac{5-20 \text{ meV} \quad 18-36 \text{ nm}}{155 \text{ meV} \quad 7 \text{ nm}}\\ \text{Field contribution} \quad \frac{5-20 \text{ meV} \quad 18-36 \text{ nm}}{155 \text{ meV} \quad 7 \text{ nm}}\\ \text{Field contribution} \quad \frac{5-20 \text{ meV} \quad 18-36 \text{ nm}}{155 \text{ meV} \quad 7 \text{ nm}}\\ \text{Field contribution} \quad \frac{5-20 \text{ meV} \quad 18-36 \text{ nm}}{155 \text{ meV} \quad 7 \text{ nm}}\\ \text{Field contribution} \quad \frac{5-20 \text{ meV} \quad 15 \text{ nm}}\\ \frac{5-20 \text{ meV} \quad 15 \text{ nm}}{155 \text{ meV} \quad 7 \text{ nm}}\\ \frac{5-20 \text{ meV} \quad 15 \text{ nm}} \\ \frac{5-20 \text{ meV} \quad 15 \text{ mm}}{155 \text{ meV} \quad 7 \text{ nm}}\\ \frac{5-20 \text{ meV} \quad 15 \text{ mm}}{155 \text{ meV} \quad 7 \text{ mm}}\\ \frac{5-20 \text{ meV} \quad 15 \text{ mm}}{155 \text{ meV} \quad 7 \text{ mm}}\\ \frac{5-20 \text{ meV} \quad 15 \text{ mm}}{155 \text{ meV} \quad 7 \text{ mm}}\\ \frac{5-20 \text{ meV} \quad 15 \text{ mm}}{150 \text{ meV} \quad 150 \text{ mm}}} \\ \frac{5-20 \text{ meV} \quad 15 \text{ mm}}{150 \text{ meV} \quad 150 \text{ mm}} \\ \frac{5-20 \text{ meV} \quad 15 \text{ mm}}{150 \text{ m}} \\ \frac{5-20 \text{ meV} \quad 15 \text{ mm}}{150 \text{ m}} \\ \frac{5-20 \text{ meV} \quad 15 \text{ mm}}{150 \text{ m}} \\ \frac{5-20 \text{ meV} \quad 15 \text{ mm}}{150 \text{ m}} \\ \frac{5-20 \text{ meV} \quad 15 \text{ mm}}{150 \text{ m}} \\ \frac{5-20 \text{ meV} \quad 15 \text{ mm}}{150 \text{ m}} \\ \frac{5-20 \text{ meV} \quad 15 \text{ mm}}{150 \text{ m}} \\ \frac{5-20 \text{ meV} \quad 15 \text{ mm}}{150 \text{ m}} \\ \frac{5-20 \text{ meV} \quad 15 \text{ mm}}{150 \text{ m}} \\ \frac{5-20 \text{ meV} \quad 15 \text{ mm}}{150 \text{ m}} \\ \frac{5-20$$

Not practical yet due to \mathcal{Q}_n Solution: take limit of T close to T_c then $\mathcal{Q}_n \approx \mathcal{Q}_0 = \pi k_B T = \pi k_B T_c$ Limit of strong field (w.r.t. $k_B T_c$) $k_1^{-1} = k_2^{-1} = \xi_F$ Limit of zero field (normal metal) $k_1^{-1} = \sqrt{\hbar D / (2\pi k_B T_c)}$ $k_2^{-2} = \infty$

What do these results imply?
stronger
$$h_{ex} \xrightarrow{\text{results in}} k_2$$
 closer to k_1 but always $k_1 \ge k_2$
decay < oscillation

To see oscillatory behavior we need:

A periode not much longer then the decay length

At best (strong field) we have $k_1^{-1} = k_2^{-1}$

But even then, the period is over 6 times the decay length

We can't expect to see many oscillations !!!

Oscillatory decay near Tc



What is the oscillation

$$\begin{array}{lll} \text{Singlet:} & \Psi^{S} = \left\langle \uparrow_{\varepsilon} \left| \downarrow_{-\varepsilon} \right\rangle - \left\langle \downarrow_{\varepsilon} \left| \uparrow_{-\varepsilon} \right\rangle \right. \end{array} \right. \\ & \text{Triplets:} \left[\begin{array}{c} \Psi^{T} & = \left\langle \uparrow_{\varepsilon} \left| \downarrow_{-\varepsilon} \right\rangle + \left\langle \downarrow_{\varepsilon} \left| \uparrow_{-\varepsilon} \right\rangle \right. \\ & \Psi^{T}_{m=1} & = \left\langle \uparrow_{\varepsilon} \left| \uparrow_{-\varepsilon} \right\rangle \\ & \Psi^{T}_{m=-1} & = \left\langle \downarrow_{\varepsilon} \left| \downarrow_{-\varepsilon} \right\rangle \end{array} \right. \end{array} \right. \end{aligned}$$

Adding the energy of the exchange field (+ phase evolution term)

$$\left|\uparrow_{\varepsilon}\right\rangle \rightarrow \left|\uparrow_{\varepsilon+h_{ex}/2}\right\rangle e^{ith_{ex}/(2h)} \qquad \left|\downarrow_{\varepsilon}\right\rangle \rightarrow \left|\downarrow_{\varepsilon-h_{ex}/2}\right\rangle e^{-ith_{ex}/(2h)}$$

Total wave function $\Psi(t) = \langle \uparrow_{h_{ex}/2} | \downarrow_{h_{ex}/2} \rangle e^{ith_{ex}/h} - \langle \downarrow_{-h_{ex}/2} | \uparrow_{-h_{ex}/2} \rangle e^{-ith_{ex}/h}$ $\Psi(t) = \Psi^{S} \cos(th_{ex}/h) + \Psi^{T} i \sin(th_{ex}/h)$

Corresponding length in diffusive system $\lambda_F = \sqrt{DT} = \sqrt{2\pi Dh/h_{ex}} = 2\pi \xi_F$

Oscillation describes the conversion between singlet and odd triplet !!

How to get long-range triplets



Kadigrobov et al. (Europhys. Lett. 54(3) 2001)

The injected Cooper pairs must consist of singlet and triplet parts

Reducing the spin-splitter thickness towards an interface, we only need nonhomogenous magnetization (ie. sampling non-co-linear magnetization directions)

FSF spin valve

Typical device layout



Theoretical model / prediction

- only co-linear magnetization
- identical spin-bands!! (no polarization)
- Parallel suppresses superconductor
 stronger than anti-parallel ... but why ??

Comparing parallel and anti-parallel (within theoretical model)

- Normal reflections at the SF interfaces have become spin independent (no contribution of QPs, for them P and AP are identical)
- \cdot The proximity effect (AR) is only different for CPs using both F layers
 - parallel always a strong de-phasing of pairanti-parallel possibility to avoid de-phasing by field

Difference between P and AP only due to de-phasing rates

stronger de-phasing leads to a more suppressed gap (superconductor)

What can we expect when non-identical spin bands are taken into account?Cooper pair confinement strongest in Parallel- stronger gap

QP density in superconductor lowest in Parallel

- stronger gap

Running experiments

